

The use and applicability of machine learning algorithms in predicting the surgical outcome for patients with benign prostatic enlargement. Which model to use?

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APPENDIX A

In what follows, assume y_1, y_2, \dots, y_n to be the predicted values on test instances and y_1, y_2, \dots, y_n to be the actual values.

- a) The correlation coefficient measures the correlation and dependence between observed values. The values range between -1 and 1, where 0 indicates no correlation, 1 a very strong positive correlation, and -1 a very strong negative correlation. The correlation coefficient measures the statistical correlation between y 's and y 's.

$$r_{yy} = \frac{\sum_{i=1}^n (y_i - \bar{y})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (y_i - \bar{y})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$$

where $\bar{y} = \frac{1}{n} \sum_{i=1}^n y_i$ and $\bar{y} = \frac{1}{n} \sum_{i=1}^n y_i$

- b) *Mean Absolute Error* (MAE) – this is an alternative calculated by the average of the individual errors without taking account of their sign. The mean-squared error tends to exaggerate the effect of outliers – instances whose prediction error is larger than the others – but the absolute error does not have this effect: all sizes of error are treated evenly according to their magnitude.

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

- c) *Root Mean-Squared Error* (RMSE) is the standard deviation of the prediction errors. The sensitivity of the RMSE to outliers is the most common concern with the use of this metric since the RMSE penalizes large errors while the MAE gives the same weight to all errors (1).

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

Concerning the values of the MAE and RMSE, the smaller their values, the better the model's performance, since both metrics are proportional to the difference between the actual and predicted values.

APPENDIX B

- 1) Linear Regression is a common statistical approach for constructing a linear model (function) predicting a value of the variable while knowing the values of the other variables. It uses the least mean square method to adjust the parameters of the linear model.
- 2) Multilayer Perceptron is performed on multi-layered neural networks, usually interconnected in a feed-forward manner, where each neuron on all layers, except the output one, feeds into the subsequent layer's neurons. The network parameters can also be monitored and modified during training time. Such networks are usually trained using an error back-propagation mechanism where the observed differences between actual and expected outputs help drive the adjustment of the weights (the connections between neurons).
- 3) SMOreg implements the support vector machine for regression (2). The parameters can be learned using various algorithms. The default algorithm (RegOptimizer) is the RegSMOImproved (3).
- 4) Instance-Based Learning (k-Nearest Neighbors) (lazy.IBk) Instance-based learning approaches (4), such as the *k-nearest neighbors* (kNN) algorithm, adopt a straightforward approach to estimate real or discrete-valued target functions (5). Predicting the output of a new input vector involves collecting and aggregating outputs from similar instances

(called “neighbors”) from the saved training data. Unlike many other techniques that create only one local approximation to the target function, an important advantage of instance-based algorithms is that the model can build a new approximation to the target function for each new query instance. This gives instance-based algorithms the ability to capture very complicated relationships between attributes and outputs. If the target variable depends only on a few of the attributes, this can cause very similar instances to be predicted at a large distance (6). In our experiments, the value of k was set to 4.

- 5) Meta-learning method “Bagging” consists of aggregating results of n models generated on the basis of n bootstrap sets. The bootstrap sets are generated using feature selection or random drawing with substitution from the original dataset. The final result is calculated by averaging the outputs of individual models built over each bootstrap set (7-9).
- 6) M5Rules. This algorithm generates a decision list for regression problems using separate-and-conquer. In each iteration, it builds a model tree and then generates a rule out of the “best” leaf. The algorithm divides the space of the parameters into subspaces and builds in each of them a linear regression model. It is based on the M5 algorithm. Once all the examples are covered, the algorithm terminates (7, 9).
- 7) M5P – Pruned Model Tree. The algorithm is based on decision trees; however, instead of having values at the tree's nodes, it contains a multivariate linear regression model at each node. The input space is divided into cells using training data and their outcomes; then, a regression model is constructed as a tree leaf in each cell (7, 10, 11).
- 8) Random forests (12) is a substantial modification of bagging that creates a large number of de-correlated trees and then averages them. On many problems, the performance of random forests is very similar to boosting, and they are simpler to train and tune.

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